#### UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

# MARK SCHEME for the May/June 2012 question paper for the guidance of teachers

## 9709 MATHEMATICS

9709/43

Paper 4, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2012 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Page 2	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2012		43

### Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2012		43

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through  $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

Page 4	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2012		43

1					
Work done is 21.9 J A1 [3]  2 (i)	1		M1		For using WD = Fdcos $\alpha$
2 (i) M1 For resolving forces horizontally or vertically $T\cos\theta + T\sin\theta = 11.2 \\ (or - T\cos\theta + T\sin\theta = 0.16g)$ $- T\cos\theta + T\sin\theta = 0.16g \\ (or T\cos\theta + T\sin\theta = 11.2) $ A1 [3]  (ii) $[T\cos\theta = 4.8 \text{ and } T\sin\theta = 6.4 \text{ and } \\ T^2 = 4.8^2 + 6.4^2 \text{ or } \tan\theta = 6.4/4.8] \\ [4T^2(\cos^2\theta + \sin^2\theta) = \\ (11.2 - 1.6)^2 + (11.2 + 1.6)^2 \\ or 2T\sin\theta \div 2T\cos\theta = \\ (11.2 + 1.6) \div (11.2 - 1.6) \\ or (T\cos\theta + T\sin\theta) \div (-T\cos\theta + T\sin\theta) \\ = 11.2 \div 1.6] $ M1 $T = 8 \text{ (or } \theta = 53.1) $ A1 $\theta = 53.1 \text{ or } T = 8 $ A1 [3]  3 (i) M1 For using $s = \int v dt$ $s = 0.027[10 000/3 - 10000/4] $ DM1 For finding the value of $t$ at A and using limits or equivalent Distance is 22.5 m A1 [4]		$WD = 6 \times (0.5 \times 8)\cos 24^{\circ}$	A1		
vertically $T\cos\theta + T\sin\theta = 11.2 \\ (or - T\cos\theta + T\sin\theta = 0.16g)$ $- T\cos\theta + T\sin\theta = 0.16g \\ (or T\cos\theta + T\sin\theta = 11.2)$ A1 [3]  (ii) $[T\cos\theta = 4.8 \text{ and } T\sin\theta = 6.4 \text{ and } \\ T^2 = 4.8^2 + 6.4^2 \text{ or } \tan\theta = 6.4/4.8] \\ [4T^2(\cos^2\theta + \sin^2\theta) = \\ (11.2 - 1.6)^2 + (11.2 + 1.6)^2 \\ or 2T\sin\theta \div 2T\cos\theta = \\ (11.2 + 1.6) \div (11.2 - 1.6) \\ or (T\cos\theta + T\sin\theta) \div (-T\cos\theta + T\sin\theta) \\ = 11.2 \div 1.6]$ M1 $T = 8 \text{ (or } \theta = 53.1)$ $\theta = 53.1 \text{ or } T = 8$ A1 [3]  3 (i)  M1  For using $s = \int vdt$ $s = 0.027(10t^3/3 - t^4/4)  (+C)$ $s = 0.027[10 000/3 - 10000/4]$ DM1  For finding $T\cos\theta$ and $T\sin\theta$ and hence finding $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\sin\theta$ and $T\cos\theta$ and $T\sin\theta$ and		Work done is 21.9 J	A1	[3]	
(or $-\text{Tcos}\theta + \text{Tsin}\theta = 0.16\text{g}$ (or $-\text{Tcos}\theta + \text{Tsin}\theta = 0.16\text{g}$ (and $-\text{Tcos}\theta + \text{Tsin}\theta = 0.16\text{g}$ ) (by $-\text{Tcos}\theta + \text{Tsin}\theta = 0.16\text{g}$ ) (cor $-\text{Tcos}\theta + \text{Tsin}\theta = 0.16\text{g}$ ) (co	2 (i)		M1		
(or $T\cos\theta + T\sin\theta = 11.2$ ) A1 [3]  (ii) $[T\cos\theta = 4.8 \text{ and } T\sin\theta = 6.4 \text{ and } T^2 = 4.8^2 + 6.4^2 \text{ or } \tan\theta = 6.4/4.8]$ For finding $T\cos\theta$ and $T\sin\theta$ and hence finding $T\cos\theta$ and $T\sin\theta$ and hence finding $T\cos\theta + \sin^2\theta$ or $T\cos\theta + \sin^2\theta$ in the value of $T\cos\theta + \sin\theta + 2\cos\theta = (11.2 + 1.6) \div (11.2 - 1.6)$ or $T\cos\theta + T\sin\theta$ in the value of $T\cos\theta + T\cos\theta$ in			A1		
$T^{2} = 4.8^{2} + 6.4^{2} \text{ or } \tan \theta = 6.4/4.8] $ finding T or $\theta$ , OR for finding the value of $(11.2 - 1.6)^{2} + (11.2 + 1.6)^{2}$ or $2 \text{Tsin } \theta \div 2 \text{Tcos } \theta = (11.2 + 1.6) \div (11.2 - 1.6)$ or $(12 + 1.6) \div (11.2 - 1.6)$ or $(12 + 1.6) \div (11.2 - 1.6)$ or $(13 + 1.6) \div (11.2 - 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 + 1.6) \div (13 + 1.6)$ or $(13 + 1.6) \div (13 $			A1	[3]	
T = 8 (or $\theta$ = 53.1) A1 $\theta$ = 53.1 or T = 8 A1 [3] 3 (i) M1 For using s = $\int v dt$ s = 0.027(10 $t^3/3 - t^4/4$ ) (+C) A1 s = 0.027[10 000/3 - 10000/4] DM1 For finding the value of $t$ at A and using limits or equivalent  Distance is 22.5 m A1 [4]	(ii)	$T^{2} = 4.8^{2} + 6.4^{2} \text{ or } \tan \theta = 6.4/4.8]$ $[4T^{2}(\cos^{2}\theta + \sin^{2}\theta) = (11.2 - 1.6)^{2} + (11.2 + 1.6)^{2}$ or $2T\sin\theta \div 2T\cos\theta = (11.2 + 1.6) \div (11.2 - 1.6)$			finding T or $\theta$ , OR for finding the value of $4T^2(\cos^2\theta + \sin^2\theta)$ or of $2T\sin\theta \div 2T\cos\theta$ or of
$\theta = 53.1 \text{ or } T = 8$ A1 [3]  3 (i)  M1 For using $s = \int v dt$ $s = 0.027(10t^3/3 - t^4/4)$ (+C)  A1 $s = 0.027[10\ 000/3 - 10000/4]$ DM1 For finding the value of $t$ at A and using limits or equivalent  Distance is 22.5 m A1 [4]		$= 11.2 \div 1.6$	M1		
3 (i) M1 For using $s = \int v dt$ $s = 0.027(10t^3/3 - t^4/4)  (+C) \qquad A1$ $s = 0.027[10\ 000/3 - 10000/4] \qquad DM1 \qquad \text{For finding the value of } t \text{ at A and using limits or equivalent}$ $Distance \text{ is } 22.5 \text{ m} \qquad A1  [4]$		$T = 8 \text{ (or } \theta = 53.1)$	A1		
$s = 0.027(10t^3/3 - t^4/4)$ (+C) A1 $s = 0.027[10\ 000/3 - 10000/4]$ DM1 For finding the value of $t$ at A and using limits or equivalent  Distance is 22.5 m A1 [4]		$\theta = 53.1 \text{ or } T = 8$	A1	[3]	
$s = 0.027[10\ 000/3 - 10000/4]$ DM1 For finding the value of $t$ at A and using limits or equivalent  Distance is 22.5 m A1 [4]	3 (i)		M1		For using $s = \int v dt$
limits or equivalent  Distance is 22.5 m A1 [4]		$s = 0.027(10t^3/3 - t^4/4) \qquad (+C)$	A1		
L J		$s = 0.027[10\ 000/3 - 10000/4]$	DM1		
(ii) $[0.027(20t - 3t^2) = 0 \implies t = 20/3]$ ] M1 For using $dv/dt = 0$		Distance is 22.5 m	A1	[4]	
	(ii)	$[0.027(20t - 3t^2) = 0 \implies t = 20/3]]$	M1		For using $dv/dt = 0$
$v_{\text{max}} = 0.027(4000/9 - 8000/27)$ A1ft ft incorrect t in $0.027(10t^2 - t^3)$		$v_{\text{max}} = 0.027(4000/9 - 8000/27)$	Alft		ft incorrect t in $0.027(10t^2 - t^3)$
		Maximum speed is 4 ms <sup>-1</sup>	A1	[3]	

Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2012		43

4	(i)	[When $4 < v < 6$ , $a_{ave} = (6-4)/(0.5-0)$ ; when $19 < v < 21$ $a_{ave} = (21-19)/(24.5-16.3)$ ]	M1		For using $a \approx \frac{\Delta v}{\Delta t}$	
		Average accelerations are 4 ms <sup>-2</sup> and 0.244 ms <sup>-2</sup>	A1	[2]		
(1	(ii)	DF(5) = P/5 and $DF(20) = P/20$	B1			
		[DF - R = ma]	M1		For using Newton's 2 <sup>nd</sup> law	
		$P/5 - R = 1230 \times 4$ and $P/20 - R = 1230 \times 0.244$	A1ft		ft incorrect average a values	
		P = 30800 (or $R = 1240$ )	B1			
		R = 1240 (or $P = 30800$ )	B1ft	[5]	ft $P/5 - 1230a_1$ or $P/20 - 1230a_2$ or $5(1230a_1 + R)$ or $20(1230a_2 + R)$	
5	(i)	WD against resistance = $800 \times 500$	B1			
		[2 800 000 = PE gain + 400 000]	M1		For using WD by the driving force = PE gain + WD against resistance	
		$[2400\ 000 = 16000g \times 500\sin\alpha]$	M1		For using PE gain = mgLsin $\alpha$	
		$\alpha = 1.7$	<b>A</b> 1	[4]		
(1	ii)	[KE gain = 2400000 + 2400000 - 800000]	M1		For using KE gain = WD by the driving force + PE loss – WD against resistance	
		4000 000 J	A1ft		ft PE gain	
		$[ \frac{1}{2} 16000(v^2 - 20^2) = 40000000]$	M1		For KE gain = $\frac{1}{2}$ m( $v^2 - 20^2$ ) and attempting to solve for $v$	
		Speed is 30 ms <sup>-1</sup>	<b>A</b> 1	[4]		
<b>justi</b> l Uses	SR (max 2/4) for candidates who assume constant driving force and constant resistance without justification Uses Newton's Second Law and $v^2 = u^2 + 2as$ [4800 + 16000gsin $\alpha - 1600 = 16000a$ , $v^2 = 20^2 + 2a \times 500$ )] M1 Speed is 30 ms <sup>-1</sup> A1					
		Alternative Method for Part (i)				
	(i)	Driving force = $2800\ 000 \div 500$ [DF - mgsin $\alpha$ - R = m × 0] For using Newton's second law	B1 M1			
		[ $16000 \times 10\sin\alpha = 5600 - 800$ ] For solving the resultant equation for $\alpha$ $\alpha = 1.7$	DM1 A1	[4]		

Page 6	age 6 Mark Scheme: Teachers' version		Paper
	GCE AS/A LEVEL – May/June 2012	9709	43

6 (i)		M1		For resolving forces parallel to the plane
	$F = 5.9 - 6.1 \sin \alpha$	A1		
	$R = 6.1\cos\alpha$	B1		
	$[5.9 - 6.1 \sin \alpha \le \mu (6.1 \cos \alpha)]$	M1		For using $F \le \mu R$
	$\mu > \frac{4}{5}$	A1	[5]	AG
(ii)	$[6.1 \times (11/61) + 5.9 - \mu 6.1 \times (60/61) > 0]$	M1		For using $F = \mu R$ and 'net downward force > 0'
	$\mu < \frac{7}{6}$	A1	[2]	AG
(iii)	$[6.1 \times (11/61) + 5.9 - \mu \ 6.1 \times (60/61) = 0.61 \times 1.7]$	M1		For using Newton's $2^{nd}$ law and $F = \mu R$
	$\mu = 0.994$	<b>A</b> 1	[2]	
7 (i)				For using Newton's second law
	[T - 0.12g = 0.12a & 0.38g - T = 0.38a; $a = \frac{0.38 - 0.12}{0.38 + 0.12}g$ ]	M1		for A and B or for using $a = \frac{M - m}{M + m}g$
	Acceleration is 5.2 ms <sup>-2</sup>	A1	[2]	
(ii)	$[v^2 = 2 \times 5.2 \times 0.65; 0.65 = \frac{1}{2} 5.2 T_B^2]$	M1		For using $v^2 = 2ah$ or $s = \frac{1}{2}at^2$
	Speed of B is $2.6 \text{ms}^{-1}$ or $T_B = 0.5$	A1ft		ft incorrect a
	$T_B = 0.5$ or Speed of B is $2.6 \text{ms}^{-1}$	B1	[3]	
(iii)	[-2.6 = 2.6 - 10(T - 0.5)]	M1		For using $-V = V - g(T - T_B)$ or equivalent
	T = 1.02	A1ft		ft incorrect V and/or T <sub>B</sub>
	Correct graph for $0 < t < 1.02$ ft incorrect values of V, T and $T_B$	B1ft	[3]	0.5 1.02
(iv)	[0.65 + 0.5(1.02 - 0.5)2.6]	M1		For using 'total distance = $\frac{1}{2} (VT_B) + 2 \times \frac{1}{2} \frac{T_A - T_B}{2} V$
	Total distance is 1.326 m (accept 1.33)	A1	[2]	